

## 3D Vector Math Menu

This menu implements a 3D Vector stack to perform operations and functions over it. To show it, touch the “**OPT**” key, and in the “**1) Scientific:**” section touch the “**3D Vector Math**” button.

	X-axis	Y-axis	Z-axis
Vt	+0.00	+0.00	+0.00
Vz	+4.00		+5.00
Vy	+1.69		-13.54
Vx	+3.00	-2.00	+5.00

3D Vector Stack Display

The interface includes the following buttons:

- X,Y,Z → (x,y,z)
- F(v)
- X↑
- Y↑
- Z↑
- CHS
- R↓
- R↑
- X≤Y
- LstV
- CLV
- |Vx|
- dot
- Scale
- ×
- 
- +

This 3d Vector-Stack is similar to the normal calculator’s stack, but specially designed for operations with vectors. The numbers entered in the Vector Stack from the calculator using the [→in] button, the calculator’s stack-X value is used as the vector X coordinate, the value in stack-Y is used for the vector Y coordinate and the value in the stack-Z is used for the vector Z coordinate.

The Vector Stack, operations and functions are completely independent from the calculator and behaves in RPN logic as well.

### 3D Vector Math Buttons

3D Vector Stack Display	Touch the 3D Vector Stack Display to choose the coordinates: Cartesian, Spherical or Cylindrical.
<b>[X,Y,Z▶(x,y,z)]</b>	Inputs the Vx vector components from the calculator's stack X, Y and Z. After, drops the calculator's stack three times.
<b>[ F(v)▶ ]</b>	Shows up a set of functions buttons to apply to the Vx vector.
<b>[ X↑ ]</b>	Outputs the X-axis coordinate of Vx to the calculator's stack.
<b>[ Y↑ ]</b>	Outputs the Y-axis coordinate of Vx to the calculator's stack.
<b>[ Z↑ ]</b>	Outputs the Z-axis coordinate of Vx to the calculator's stack.
<b>[CHS]</b>	Change the sign of x, y and z coordinates of the Vx vector.
<b>[R↓]</b>	Rolls Down the vector-stack.
<b>[R↑]</b>	Rolls Up the vector-stack.
<b>[X↔Y]</b>	Swaps the Vx and Vy vectors.
<b>[LstV]</b>	Recalls the last Vx vector that was just before a Function or operation was performed.
<b>[CLX]</b>	Clears the Vx vector to (0,0,0).
<b>[  Vx  ]</b>	Calculates the Modulus of the Vx vector and enters the result in the calculator's stack-X.

### 3D Vector Math Buttons

<b>[ dot ]</b>	Calculates the dot product of $V_y$ and $V_x$ vectors. The result in the calculator's stack-X.
<b>[ Scale ]</b>	Stores the $V_x$ vector in 'LstV' and Multiplies the $V_x$ vector by the calculator's stack-X value.
<b>[ x ]</b>	Cross Product $V_y$ by $V_x$ . Stores $V_x$ in 'LstV', drop the vector stack and put the result of $V_y \otimes V_x$ in $V_x$ .
<b>[ - ]</b>	Subtracts $V_x$ from $V_y$ . Stores $V_x$ in 'LstV', drop the vector stack and put the result of $V_y - V_x$ in $V_x$ .
<b>[ + ]</b>	Adds $V_y$ and $V_x$ . Stores $V_x$ in 'LstV', drop the vector stack and put the result of $V_y + V_x$ in $V_x$ .
<b>[ <math>\angle</math> Y,X ]</b>	Calculates the angle between $V_y$ and $V_x$ vectors. Enters the result in stack-X.
Touching the <b>[ F(v) ]</b> button, shows additional Functions:	
<b>[ <math>\pm</math> <math>V_y, V_x</math> ]</b>	Change the sign of all three coordinates of the $V_x$ vector.
<b>[Unit <math>V_x</math>]</b>	Stores $V_x$ in 'LstV' and calculates the directional cosines of $V_x$ vector.
<b>[ <math>V_x</math> Angles ]</b>	Enters in the calculator's stack the angles of the $V_x$ with the X,Y and Z-axis coordinates.
<b>[ <math>V_y \cdot V_x</math> ]</b>	Stores $V_x$ in 'LstV' and calculates the projection of $V_y$ vector over the $V_x$ vector.

### 3D Vector Math Buttons

<b>[ X-axis ↻ ]</b>	Rotates Vx vector around the X-axis in the angle of stack-X value.
<b>[ Y-axis ↻ ]</b>	Rotates Vx vector around the Y-axis in the angle of stack-X value.
<b>[ Z-axis ↻ ]</b>	Rotates Vx vector around the Z-axis in the angle of stack-X value.

#### Example 1:

Determine the angles that vector (3, -2, 5) forms with the coordinates axis X, Y and Z.

#### Solution:

<b>5 [ENTER] 2 [CHS]</b> <b>[ENTER] 3</b> <b>[X,Y,Z▶(x,y,z)]</b>	Enter the vector (3,-2,5) into the vector Stack.
<b>[ F(v) ]</b> <b>[ Vx Angles ]</b>	Calculates the angles in the current angle units. <b>Result :</b> (DEG angle mode) calculator's stack <b>X = 60.88</b> with X-axis. calculator's stack <b>Y = 108.93</b> with Y-axis. calculator's stack <b>Z = 35.80</b> with Z-axis.

#### Example 2:

A vector AB is directed from point A(-1, -2, 1) to point B(-2, 3, 4), find the Angle between A and B and the unit vector of the vector AB.

## Solution:

Keystrokes	Description
4 [ENTER] 3 [ENTER] 2 [CHS] [X,Y,Z▶(x,y,z)]	Enter the vector B(-2, 3, 4) into the vector Stack.
1 [ENTER] 2 [CHS] [ENTER] 1 [CHS] [X,Y,Z▶(x,y,z)]	Enter the vector (-1, -2, 1) into the vector Stack.
[↵ Vy, Vx]	Calculates the angle between A and B vectors. <b>Result: 90.00</b> (DEG angle mode)
[ - ]	Calculates vector AB.
[ F(v) ] "Vx Unit Vector"	Calculates the Unit vector of AB. <b>Result :</b> coordinate <b>X = -0.1690</b> coordinate <b>Y = 0.8452</b> coordinate <b>Z = 0.5071</b>

## Example 3:

Calculate the cross product of a vector in spherical coordinates (5, 60°, 45°) with a vector in cylindrical coordinates (8, 22°, 3). Show the result in cartesian, spherical and cylindrical coordinates :

## Solution: (assumes FIX 2 number format)

Keystrokes	Description
3D Vector Stack Display 'Spherical'	Touch the display to set display format to Spherical coordinates.

Keystrokes	Description
45 [ENTER] 60 [ENTER] 5 [X,Y,Z]►(x,y,z)]	Enters the vector (5, 60°, 45°) in spherical coordinates into the vector stack.
3D Vector Stack Display 'Cylindrical'	Touch the display to set display format to Cylindrical coordinates.
3 [ENTER] 22 [ENTER] 8 [X,Y,Z]►(x,y,z)]	Enters the vector (8, 22°, 3) in cylindrical coordinates into the vector stack.
[ x ]	Calculates the Cross Product. <b>Cylindrical</b> coordinates <b>Result:</b> coordinate <b>R = 9.51</b> coordinate <b>Φ = 79.74°</b> coordinate <b>Z = -13.54</b>
3D Vector Stack Display 'Spherical'	<b>Spherical</b> coordinates <b>Result:</b> coordinate <b>R = 16.54</b> coordinate <b>θ = 144.91°</b> coordinate <b>Φ = 79.74°</b>
3D Vector Stack Display 'Cartesian'	<b>Cartesian</b> coordinates <b>Result :</b> coordinate <b>X = 1.69</b> coordinate <b>Y = 9.36</b> coordinate <b>Z = -13.54</b>