

# Rhumb Line Worksheet

Rhumb Line			Clear
P#	LAT (°)	LON (°)	Add
1	40.60	73.70	Ins
2	33.90	118.40	Del
From ▶ P#1		To ▶ P#2	
		Rhumb Line Distance <b>2,171.28</b> NM	
True Course <b>TCrs = 259</b> °		Great Circle Distance <b>2,150.32</b> NM	

<b>Clear</b>	Remove all points leaving the initial one and clears all values to 0.
<b>P#</b>	Geographical points index column.
<b>LAT</b>	Latitude coordinate of each point (touch to change units).
<b>LON</b>	Longitude coordinate of each point (touch to change units).
<b>Add</b>	Appends a new point (latitude, longitude).
<b>Ins</b>	Insert a new point (latitude, longitude) before the selected point.
<b>Del</b>	Deletes the selected point (latitude, longitude).
<b>From▶</b>	Select the initial point (latitude, longitude) of the trip segment.
<b>To▶</b>	Select the end point (latitude, longitude) of the trip segment.
<b>Dist</b>	Recalls to the display the distance over the Rhumb Line from the <b>“From”</b> selected point to the <b>“To”</b> selected point.
<b>GCD</b>	Recalls to the display the shortest distance (Great Circle distance) from the <b>“From”</b> selected point to the <b>“To”</b> selected point.
<b>TCrs</b>	Recalls to the display the true course required for flight over the Rhumb Line.

**NOTE:** Tap the **LAT** or **LON** heading to select the coordinates units: Decimal degrees (°), Degree-Minute-Second (DMS) or radians (RAD).

The Rhumb Line function allows you to compute the true course (**TCrs**), the distance (**Dist**) of the Rhumb Line and the distance (**GCD**) in the great circle between multiple points (LAT, LON).

**NOTE: Always verify the physical units**

To change the units of a variable, tap over the unit symbol and select the right one from the pop-up menu. To change the whole units in the worksheet select “Set Metric Units” or “Set US Units” from the [ **UNITS▶** ] button in the Navigation Bar.

All the following examples use US units. So please select “Set US Units” from the [ **UNITS▶** ] menu in the Navigation Bar.

**Example 1:**

What is the true course and distance between JFK (40.6°, 73.7°) and LAX (33.9°, 118.4°)?.

Solution:

Keystrokes	Description
[ <b>Clear</b> ]	Clears all variables to start a new calculation.
type 40.6 touch P#1 LAT cell	Set latitude to 40.6° for point #1.
type 73.7 touch P#1 LON cell	Set longitude to 73.7° for point #1.
[ <b>Add</b> ]	Append point #2 to the list
type 33.9 touch P#2 LAT cell	Set latitude to 33.9° for point #2.
type 118.4 touch P#2 LON cell	Set longitude to 118.4° for point #2.
[ <b>To▶</b> ] Point 2	The initial point is already set to “Point 1” so, select the end point from the <b>To▶</b> menu to “Point 2” and the result is calculated automatically: <b>TCrs = 259 °</b> (True Course). <b>Dist = 2,171.28 NM</b> (Rhumb Line Distance). <b>GCD = 2,150.32 NM</b> (Great Circle Distance).

# Appendix : Equations Used

The equations that this worksheet calculates are:

Leg Between Point 1 ( Lat<sub>1</sub> , Lon<sub>1</sub> ) and Point 2 ( Lat<sub>2</sub> , Lon<sub>2</sub> ):

$$\Delta\text{LonW} = \text{MOD}(\text{Lon}_2 - \text{Lon}_1, 2\pi)$$

$$\Delta\text{LonE} = \text{MOD}(\text{Lon}_1 - \text{Lon}_2, 2\pi)$$

$$\Delta\text{Lon} = \text{MIN}(\Delta\text{LonW}, \Delta\text{LonE})$$

$$\Delta\text{Lat} = \text{LN}(\text{TAN}(\text{Lat}_2 / 2 + \pi/4) / \text{TAN}(\text{Lat}_1 / 2 + \pi/4))$$

$$q = (\text{Lat}_1 \neq \text{Lat}_2) ? (\text{Lat}_2 - \text{Lat}_1) / \Delta\text{Lat} : \text{COS}(\text{Lat}_1)$$

$$\text{TCrs} = 2\pi - \text{MOD}(\text{ATAN2}(\Delta\text{Lat}, \Delta\text{Lon}), 2\pi)$$

$$\text{Dist} = \sqrt{[q^2 \cdot \Delta\text{Lon}^2 + (\text{Lat}_2 - \text{Lat}_1)^2]} \cdot R_E$$

$$\text{GCD} = \text{ACOS}[\text{SIN}(\text{Lat}_1) \cdot \text{SIN}(\text{Lat}_2) + \text{COS}(\text{Lat}_1) \cdot \text{COS}(\text{Lat}_2) \cdot \text{COS}(\text{Lon}_2 - \text{Lon}_1)] \cdot R_E$$

Where:

$R_E$  = 6,371 (Km) -> Standard Radius of the Earth